Raman Spectroscopy

Part II: Rotational Raman spectroscopy

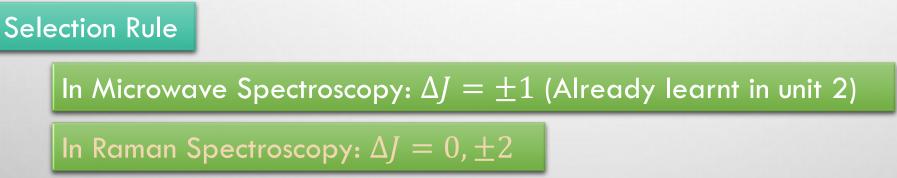
B.Sc. (H) Chemistry

Dr Anil Kumar Singh Department of Chemistry Mahatma Gandhi Central University Correction in last PPT, Raman Spectroscopy, Part-I, Slide No. 11, Molecular Polarizability The corrected version is following,

We know the trigonometric expression, sin A sin B = $\frac{1}{2} \{ \cos(A - B) - \cos(A + B) \}$ $\mu = (\alpha_0 + \beta \sin 2\pi v_{vib} t) E_0 \sin 2\pi v t$ $\mu = \alpha_0 E_0 \sin 2\pi v t + \beta \sin 2\pi v_{vib} t \cdot E_0 \sin 2\pi v t$ $\mu = \alpha_0 E_0 \sin 2\pi \nu t + \frac{1}{2} \beta E_0 \{\cos 2\pi (\nu - \nu_{vib}) - \cos 2\pi (\nu + \nu_{vib}) t\}$ $\mu = \alpha_0 E_0 \sin 2\pi \nu t + \frac{1}{2}\beta E_0 \{\cos 2\pi (\nu - \nu_{vib}) - \frac{1}{2}\beta E_0 \cos 2\pi (\nu + \nu_{vib}) t\}$ **Rayleigh Scattering** Stokes line Antistokes line

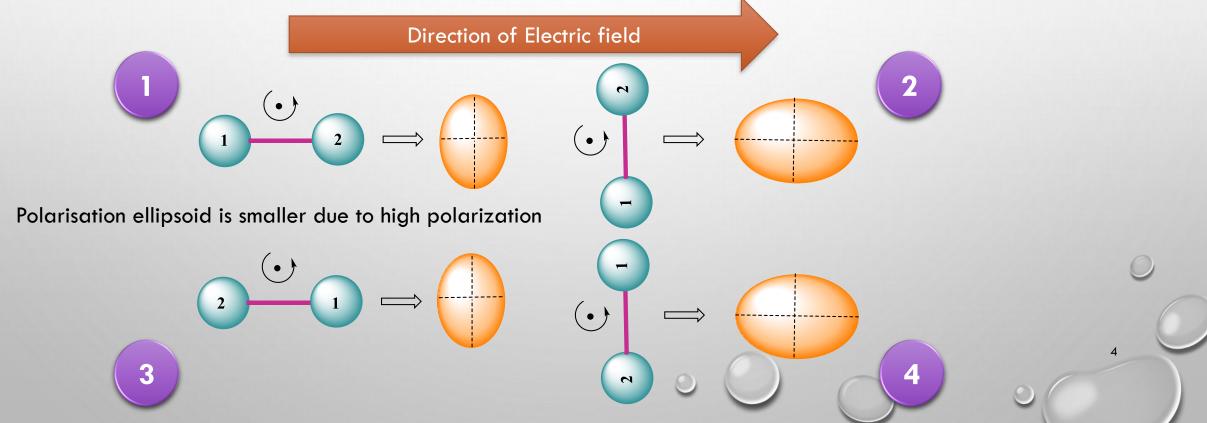
Rotational energy level of linear molecules is $\varepsilon_J = BJ(J+1) - DJ^2(J+1)^2 \text{ cm}^{-1} \qquad (J=0,1,2....)$

Neglecting the centrifugal distribution constant, D, the expression will be: $\varepsilon_J = BJ(J+1) \text{ cm}^{-1}$ (J=0,1,2.....)



In Raman spectroscopy the rotational quantum number changes by two units rather than one is connected with the symmetry of the polarizability ellipsoid.

- For a linear molecule, it is evident that during end-over-end rotation the ellipsoid presents the same appearance to an observer *twice* in every complete rotation.
- Rotation about the bond axis produces no change in polarizability.
- Only end-over-end rotations give the spectra.



For a pure rotational change, the transition,

 $\Delta J = -2$, can be ignored, so the upper state quantum number must necessarily be greater than that in the lower state.

 $\Delta J = 0$, represents no change in the molecular energy and hence we obtain **Rayleigh** scattering only.

For the transition, $\Delta J = +2$,

$$\Delta \varepsilon = \varepsilon_{J'=J+2} - \varepsilon_{J''=J}$$

Putting the values of J in the equation,

= [B(J+2)(J+3)]-[BJ(J+1)]= $B(J^2+3J+2J+6)-BJ^2-BJ$ = $BJ^2+5BJ+6B-BJ^2-BJ$ = 4BJ+6B= B(4J+6) cm⁻¹

Since $\Delta J = +2$, we may label these lines **S branch lines** and write, $\Delta \varepsilon_s = B(4J+6) \text{ cm}^{-1}$ (J = 0,1,2....)

where, \boldsymbol{J} is the rotational quantum number in the lower state.

If the molecule gains rotational energy from the photon during collision we have a series of **S** branch lines to the low wavenumber side of the exciting line (Stokes' lines), while if the molecule loses energy to the photon the **S** branch lines appear on the high wavenumber side (anti-Stokes' lines). The wavenumbers of the corresponding spectral lines are given by:

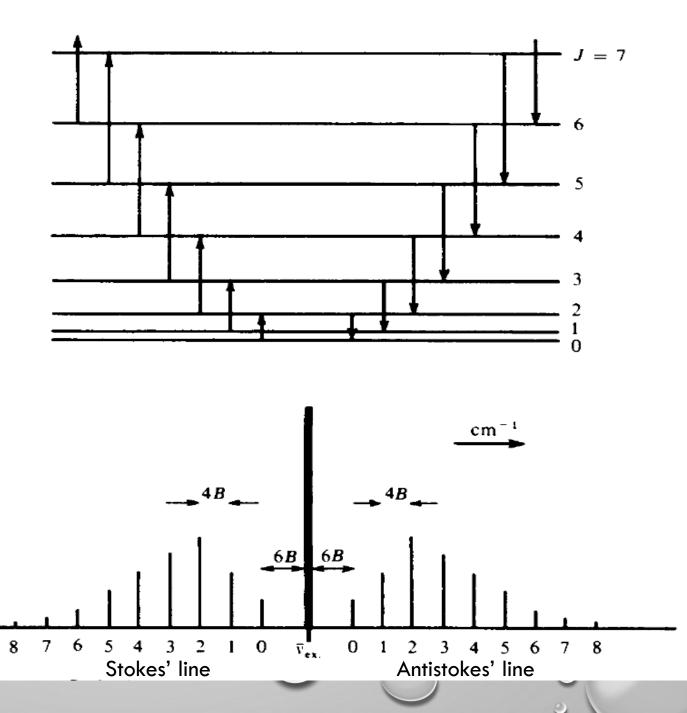
$$\overline{\nu}_{S} = \overline{\nu}_{ex.} \pm \Delta \varepsilon_{S} = \overline{\nu}_{ex.} \pm B(4J+6) \text{ cm}^{-1}$$

where the **plus** sign refers to anti-Stokes' lines, the **minus** to Stokes' lines, and \overline{v}_{ex} is the wavenumber of the exciting radiation.

If,
$$\overline{v}_S = \overline{v}_{ex.}$$
 Rayleigh line

When the value J = 0, in the equation,

 $\bar{v}_S = \bar{v}_{ex.} \pm B(4J+6) \ cm^{-1}$ it is seen immediately that the separation of the first line from the exciting line is 6B cm⁻¹, while the separation between successive lines is 4B cm⁻¹.



Picture credit: **Fundamentals of Molecular Spectroscopy**, 4th Ed. By Colin N. Banwell and Elaine M. McCash

- Eor diatomic and light triatomic molecules the rotational Raman spectrum will normally
 be resolved and we can immediately obtain a value of B, and hence the moment of inertia and bond lengths for such molecules.
- Homonuclear diatomic molecules (for example O₂, H₂) give no infra-red or microwave spectra since they possess no dipole moment, whereas they **do** give a rotational Raman spectrum.
- If the molecule has a centre of symmetry (as, for example, H₂, O₂, CO₂), then the effects
 of nuclear spin will be observed in the Raman as in the infra-red.*
- Thus for O₂ and CO₂ (since the spin of oxygen is zero) every alternate rotational level is absent;
- For example, in the case of O_2 , every level with even J values is missing, and thus every transition labelled J = 0, 2, 4, ... is also completely missing from the spectrum.
- In the case of H₂, and other molecules composed of nuclei with non-zero spin, the spectral lines show an alternation of intensity.

*(For detailed study about the influence of Nuclear spin on IR spectra, see page no. 79, : Fundamentals of Molecular Spectroscopy, 4th Ed. By Colin N. Bañwell and Elaine M. McCash)

Reference Fundamentals of Molecular Spectroscopy, 4th Ed. By Colin N. Banwell and Elaine M. McCash

Next: Vibrational Raman Spectrą

THANK YOU THANK YOU

10